

# Submap-based Bundle Adjustment for 3D Reconstruction from RGB-D Data

Robert Maier, Jürgen Sturm, Daniel Cremers
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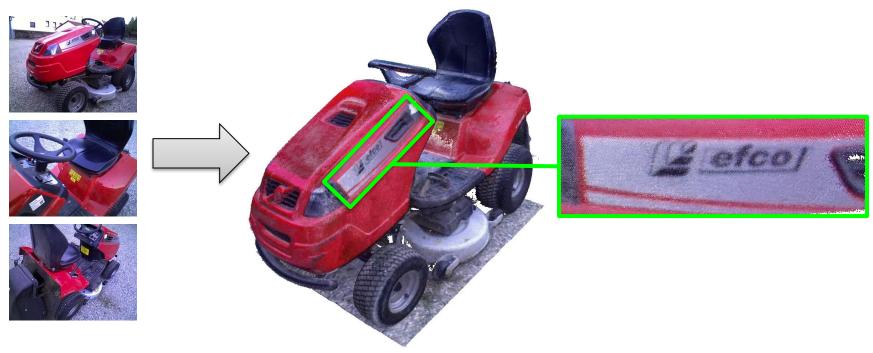


September 3, 2014



#### Motivation

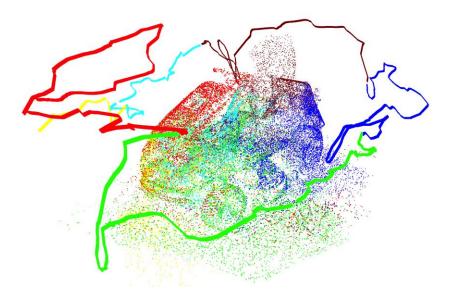
- Given: Low-cost RGB-D sensors
- Wanted: 3D reconstruction of highly accurate 3D models (e.g. for reverse-engineering)





## Submap-based Bundle Adjustment

- Problem:
  - Incremental tracking and mapping methods prone to drift
  - Full bundle adjustment (BA) too slow
- Our solution: Novel submap-based BA method for RGB-D based 3D reconstruction





#### Related Work



#### **Related Work**

- RGB-D SLAM systems
  - An evaluation of the RGB-D SLAM system [Endres et al., ICRA 2012]
  - RGB-D mapping: Using Kinect-Style Depth Cameras for Dense 3D Modeling of Indoor Environments [Henry et al., IJRR 2012]
  - Using depth in visual simultaneous localisation and mapping [Scherer et al., ICRA 2012]

Pose Graph Optimization

Sparse Bundle Adjustment

3D Bundle Adjustment



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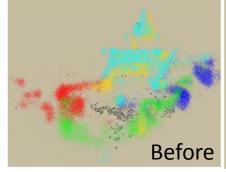
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- Out-of-core bundle adjustment for large-scale 3D reconstruction [Ni et al., ICCV 2007]

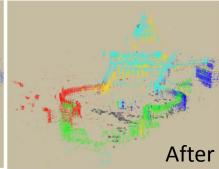
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#### Submap-based Bundle Adjustment

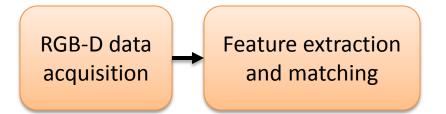






RGB-D data acquisition

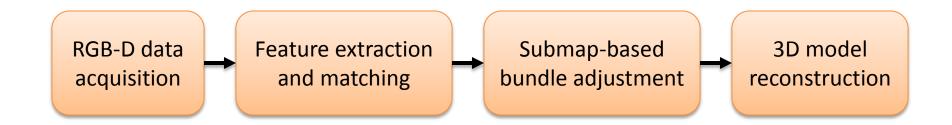








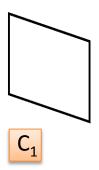








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$$(\mathbf{u}_1, \mathbf{v}_1, \mathbf{d}_1)^{\mathsf{T}} = \mathbf{z_1}$$

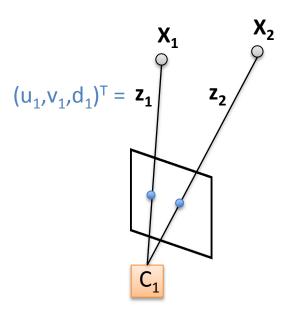
$$(\mathbf{u}_1, \mathbf{v}_1)$$

$$\mathbf{C_1}$$





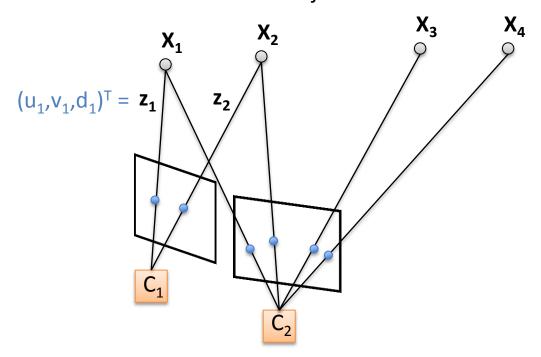
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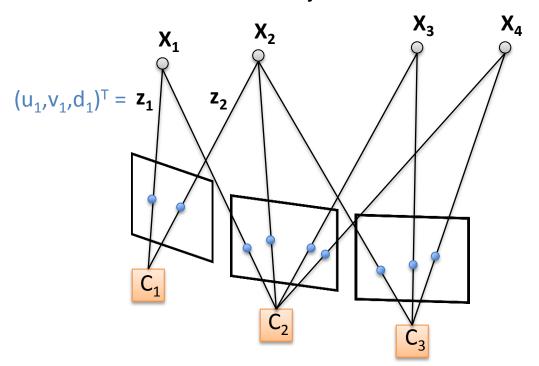
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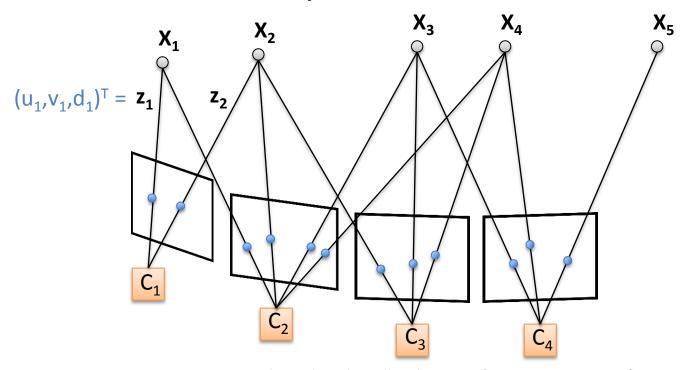


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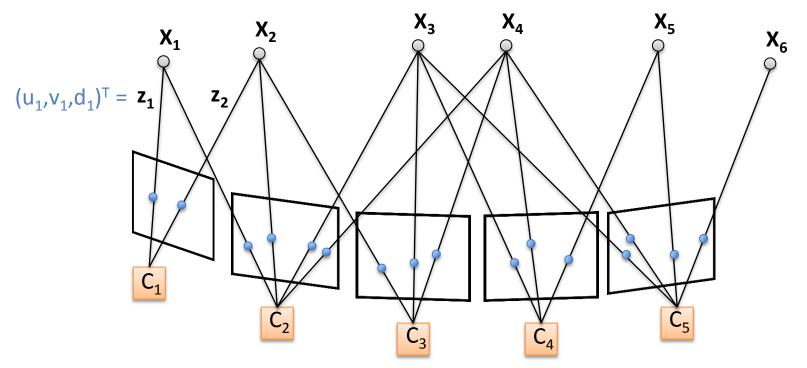


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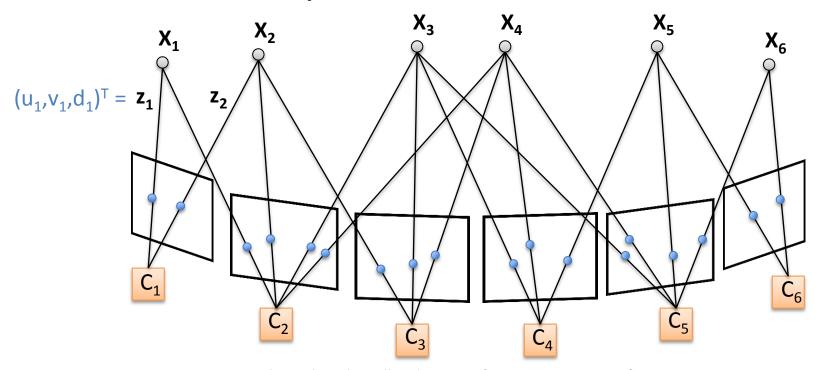


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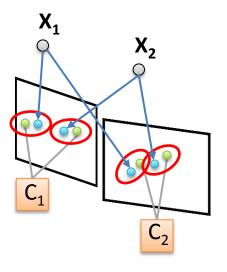




## Full Bundle Adjustment for RGB-D Sensors

#### 2D reprojection error

$$\min_{\boldsymbol{C}_{i_k}, \mathbf{X}_{j_k}} \sum_{k=1}^K ||\pi(\mathcal{T}^{-1}(\boldsymbol{C}_{i_k}, \mathbf{X}_{j_k})) - (\boldsymbol{u}_k, \boldsymbol{v}_k)^\top||^2$$







# Full Bundle Adjustment for RGB-D Sensors

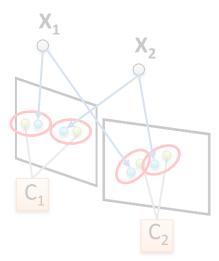
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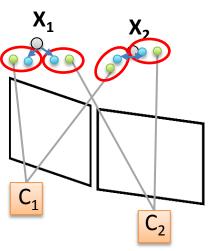
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#### 3D alignment error

$$\min_{C_{i_k}, \mathbf{X}_{j_k}} \sum_{k=1}^{K} ||\mathcal{T}^{-1}(C_{i_k}, \mathbf{X}_{j_k}) - \rho(u_k, v_k, d_k)||^2$$









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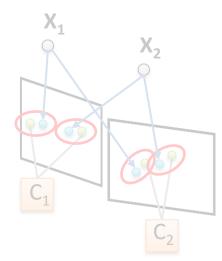
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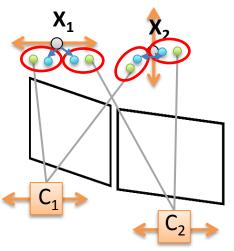
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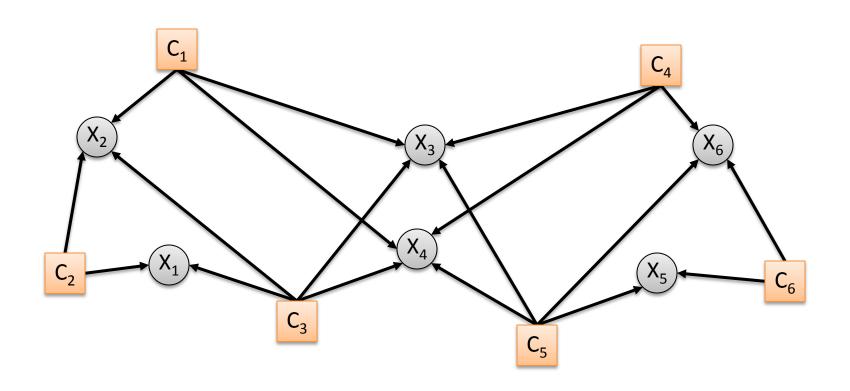


# Efficient Bundle Adjustment for RGB-D Sensors using Submapping

- 1. Graph partitioning into submaps
- 2. Submap optimization
- 3. Global submaps alignment
- 4. Submap optimization with fixed separator

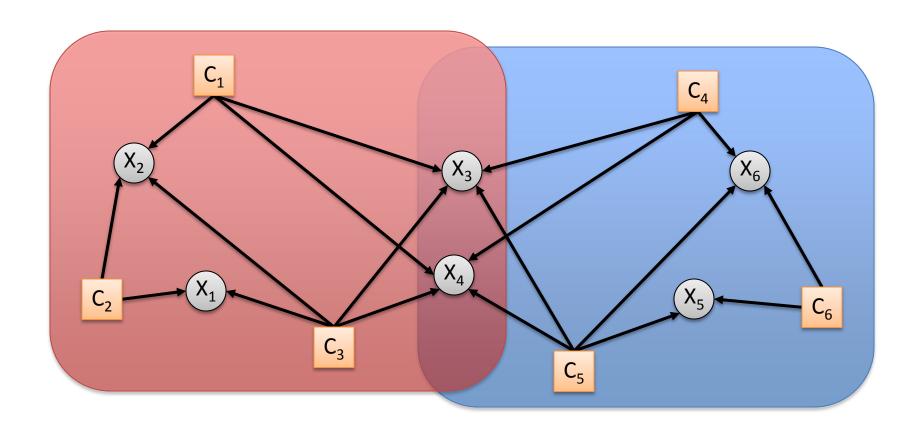






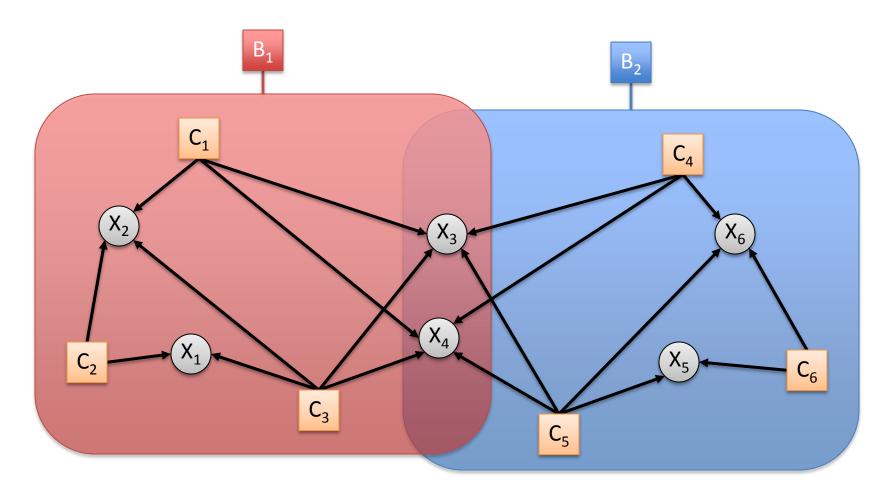






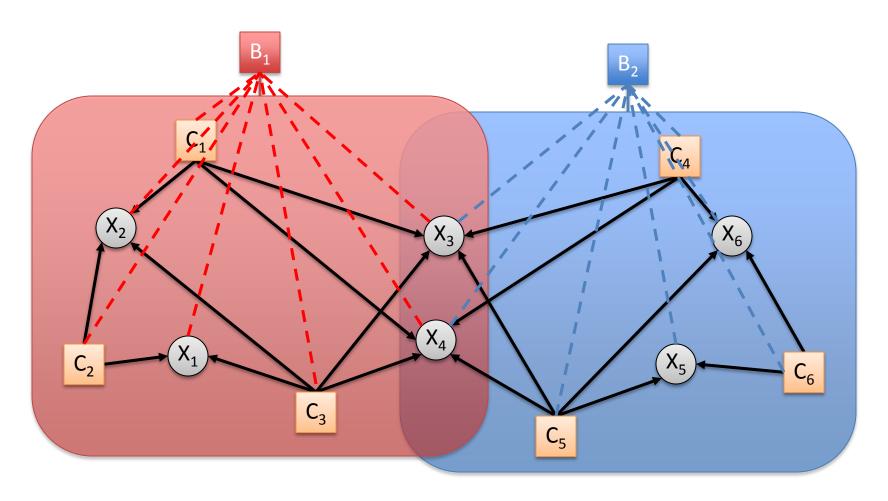








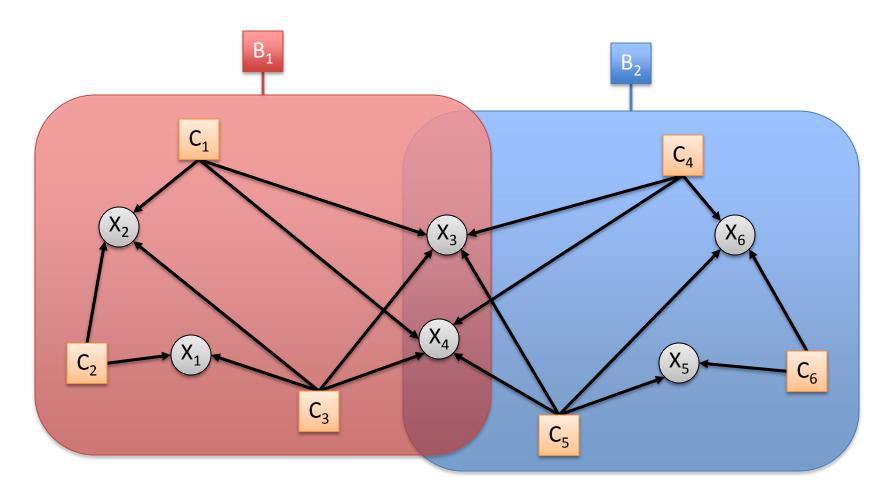








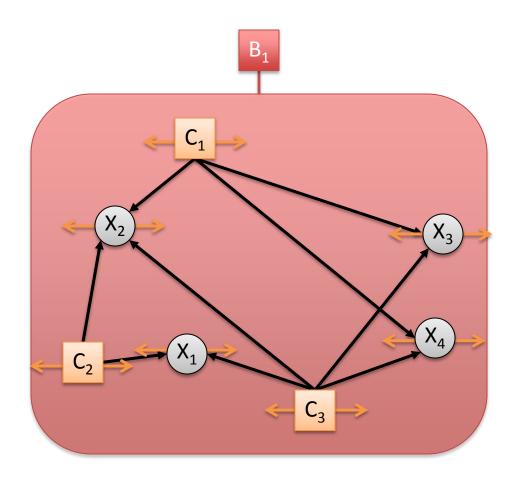
# Stage 2: Submap optimization







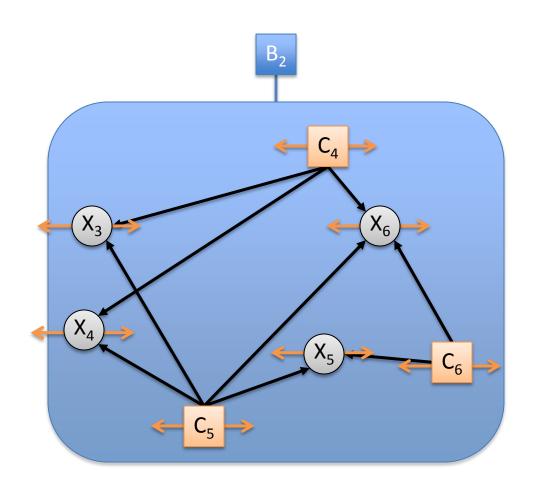
# Stage 2: Submap optimization







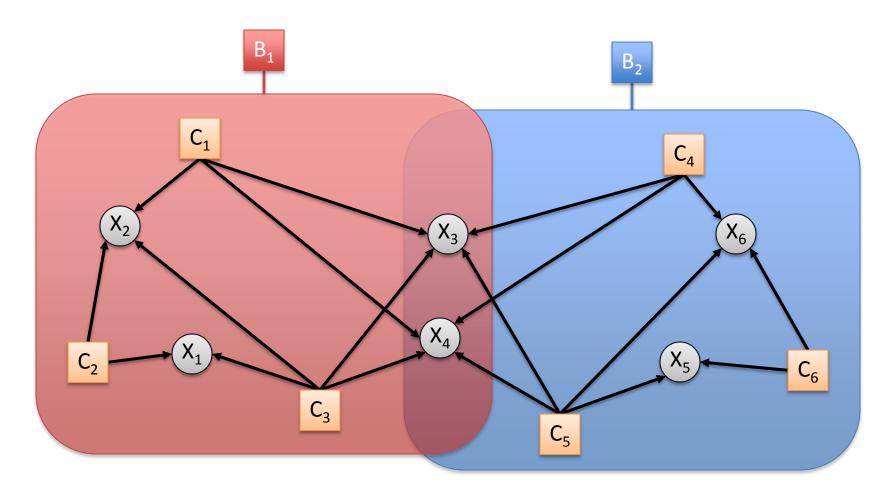
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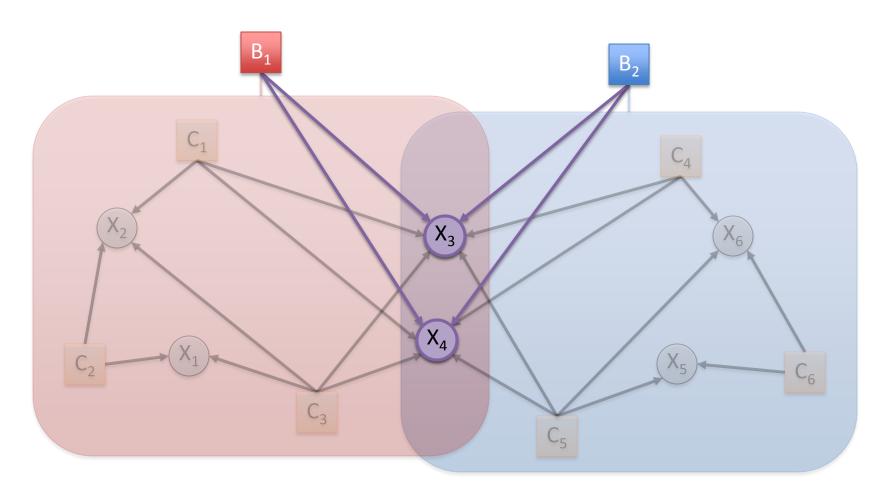
## Stage 3: Global submaps alignment







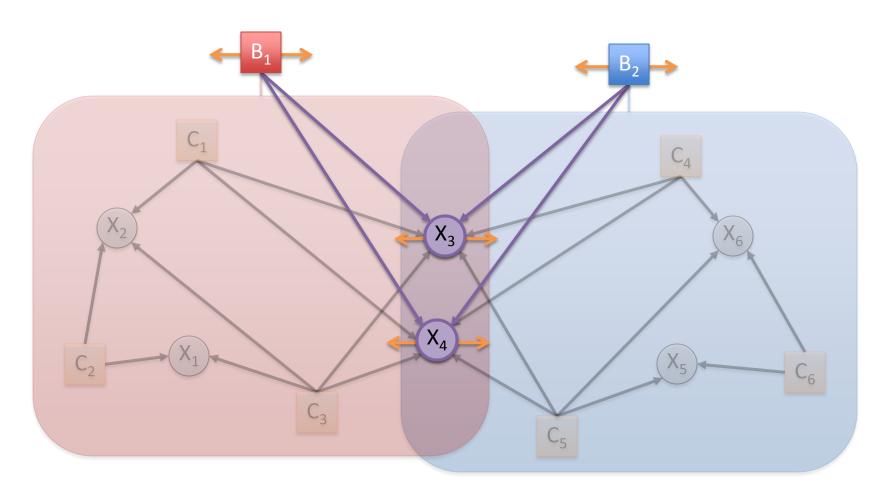
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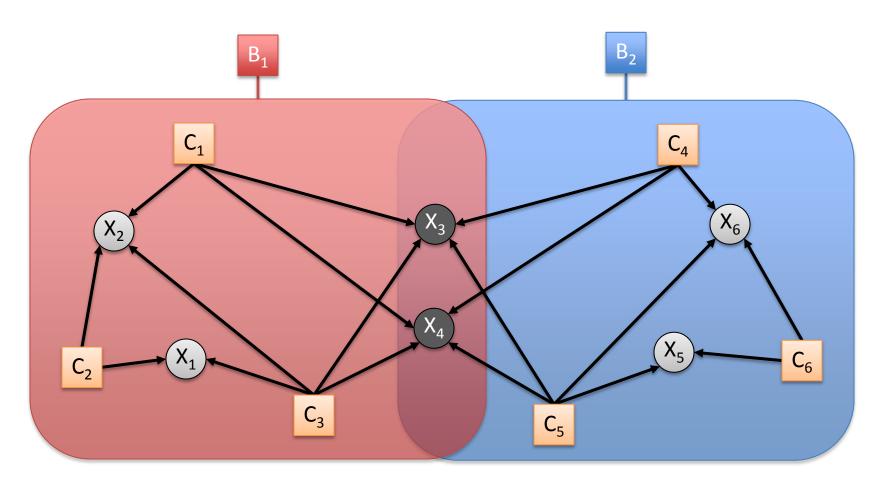
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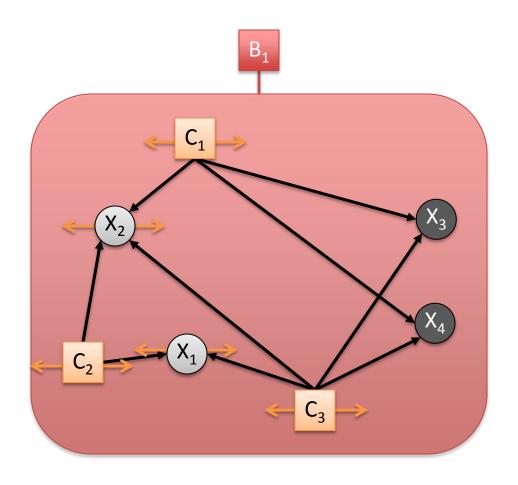
# Stage 4: Internal submap update







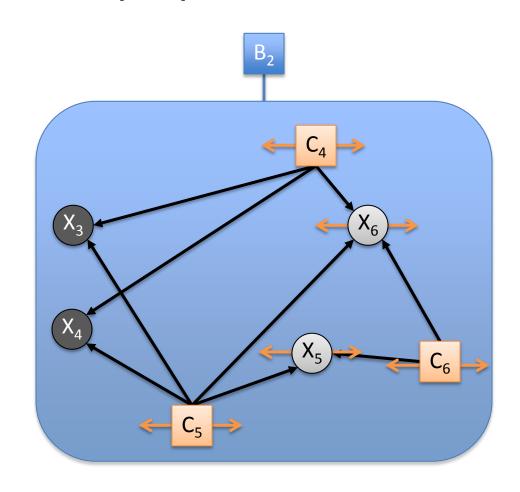
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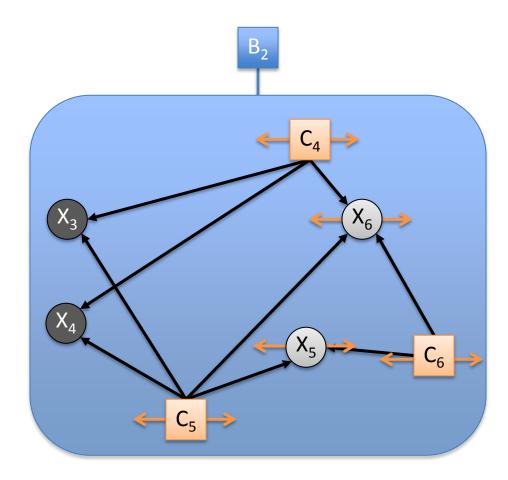
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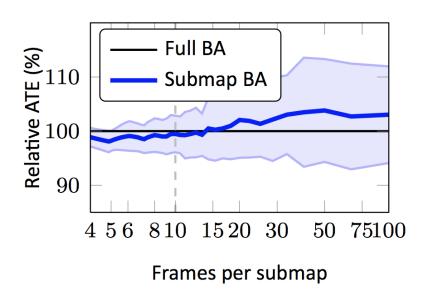
→ Use final camera poses to fuse RGB-D frames into 3D octree model

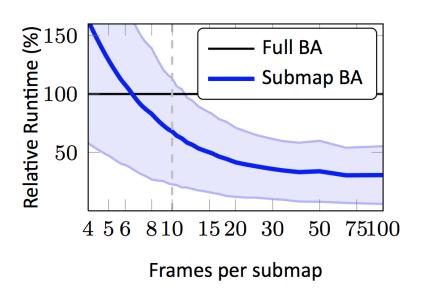


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#### **Evaluation: Size of Submaps**

 Evaluation of Absolute Trajectory Error (ATE) over 10 sequences of TUM RGB-D benchmark [Sturm et al., IROS 2012]





- Small submaps: smaller ATE than full BA
- Large submaps: increase efficiency but decrease accuracy
- Good speed/accuracy trade-off: 10 frames per submap



#### **Evaluation: Performance**

• Benchmark sequences (4 of 10 sequences):

Sequence	No BA	Full 2D	Full 3D		Submap-based 3D BA				
	ATE	ATE	ATE	time	submaps	ATE	$\pm (\%)$	time	$\pm(\%)$
FR1/desk2	0.098	0.044	0.030	27.23	62	0.031	+3.4	21.36	-21.5
FR1/room	0.275	0.228	0.085	125.46	135	0.086	+1.7	77.30	-38.4
FR2/desk	0.201	0.080	0.079	2355.26	289	0.076	-3.3	372.20	-84.2
FR3/office	0.176	0.039	0.036	1290.24	248	0.035	-3.0	242.88	-81.2
average	0.129	0.066	0.047			0.047	-0.5		-32.0

- Similar accuracy as Full 3D BA at reduced cost (-32%)
- Runtime improvement of up to 84% for long sequences
- Comparison with state-of-the-art approaches:
  - RGB-D SLAM [Endres et al., ICRA 2012]: 13% (0.047m vs. 0.054m)
  - Direct SDF tracking [Bylow et al., RSS 2013]: 17% (0.047m vs. 0.058m)



Soil auger











Soil auger













Farm tractor











Farm tractor













#### Conclusion

- Our contribution: Submap-based bundle adjustment for RGB-D data
- Global optimization exploits available depth information
- Evaluation on benchmark datasets:
  - Accuracy similar to full bundle adjustment
  - Average runtime reduced by 32%
  - Higher accuracy than other state-of-the-art approaches
- Reconstructed 3D models: compelling visual quality and metric accuracy

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#### Thank you!